# A Low-Voltage Folded-Cascode OP Amplifier with a Dynamic Switching Bias Circuit and Application to Switched Capacitor Filters 

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#### Abstract

Wideband filters employing Operational Amplifiers (OP Amps) are required in sensing devices such as video cameras for environment sensing. A high-speed lowvoltage Folded-Cascode (FC) OP Amp with a Dynamic Switching Bias (DSB) circuit capable of processing video signals, which enables low power consumption, high gain with wide bandwidths, and a wide dynamic range, was proposed. Through simulations, it was shown that the OP Amp with the reduced 3$V$ power supply is able to operate at a 14.3 MHz dynamic switching rate, allowing processing video signals, and a dissipated power of $57 \%$ compared to that in the conventional 5-V power DSBFC OP Amp while keeping a 0.6 V wide output dynamic range. The $2^{\text {nd }}$-order switched capacitor Low-Pass Filter (LPF) and the $4^{\text {th }}$-order switched capacitor LPF were tested as its applications. The response of the former was near the theoretical frequency response within frequencies below 5 MHz. The sample-hold circuit in the latter was optimized considering the feed-through phenomenon. The latter showed practical level gains in frequencies over 5 MHz within a stopband while showing a sharp roll-off near the theoretical frequency response within frequencies below 4 MHz . The power dissipation of either of these switched capacitor LPFs was also reduced to nearly $57 \%$ of that in each switched capacitor LPF with the conventional 5-V power DSBFC OP Amp.


Keywords-CMOS; operational amplifier; dynamic switching; switched capacitor circuit; filter.

## I. INTRODUCTION

This work is an extension of work originally presented in SENSORDEVICES 2018 [1]. Wideband filters are essential for signal processing in video electronic appliances. Specifically, a wideband Low-Pass Filter (LPF) is needed in sensing devices such as a CCD (Charge-Coupled Device) camera with a monitor handling a wide bandwidth video signal of over 2 MHz . The CMOS (Complementary MOS) Switched Capacitor (SC) techniques suitable for realizing analog signal processing ICs (Integrated Circuits), have promising use in video signal bandwidth circuits. It has been demonstrated that SC techniques using CMOS Operational Amplifiers (OP Amps) are useful for implementing analog functions such as filters [2]-[5]. Although CMOS OP Amps are suitable for such filter ICs, the use of several OP Amps results in large power consumption. Especially, the power consumption of OP Amps in high speed operation becomes
large because they have wideband properties. There is a possibility that this causes unstable operation.

Until now, several approaches have been considered to decrease the power consumption of OP Amps, including the development of ICs that work at low power supply voltages [6][7]. In the two-stage Folded-Cascode (FC) OP Amp operating at the low power of 1 V [7], resistive biasing and capacitive level shifter are required to increase the output voltage swing. The requirement of four resistors for the resistive biasing makes it difficult to realize as an IC. A clocked current bias scheme for FC OP Amps suitable for achieving a wide dynamic range has typically been proposed to decrease the power consumption of the OP Amp [8][9]. Since the circuit requires complicated four-phase biascurrent control pulses and biasing circuits, it is not suitable for the high speed operation and results in a large layout area.

Recently, the author proposed an FC CMOS OP Amp with a Dynamic Switching Bias circuit (DSBFC OP Amp), of simple configuration, to provide low power consumption while maintaining high speed switching operation suitable for processing video signals [10]. This OP Amp operating at the $5-\mathrm{V}$ power supply voltage is not necessarily enough for use in low-voltage signal processing applications under the progress of miniaturization of equipment. That is, the development of OP Amps with a still lower power supply voltage is expected to decrease their power dissipation.

In this paper, a Low-Voltage (LV) DSBFC OP Amp with the $3-\mathrm{V}$ power supply voltage [1] is proposed, which enables low power consumption and is suitable for achieving wide bandwidths and realizing as an IC. The point of view in design for architecture and operation of the LV DSBFC OP Amp is discussed in Section II. Simulation results for performance of the LV DSBFC OP Amp are shown in Section III. As application examples of this OP Amp, its practicability for a $2^{\text {nd }}$-order SC Butterworth LPF and a $4^{\text {th }}$ order SC Butterworth LPF is also evaluated in Section IV. Finally, conclusions of this work are summarized in Section V.

## II. LOW-Voltage DSB OP AMP CONFIGURATION

Figure 1 shows a configuration of an LV DSBFC OP Amp, in which the power supply voltages ( $\pm 1.5 \mathrm{~V}$ ) were reduced to $60 \%$ of the previous ones ( $\pm 2.5 \mathrm{~V}$ ). The DSB method is also used for implementing low power


Figure 1. Configuration of the low-voltage DSBFC OP Amp.

TABLE I. LOw-Voltage DSBFC OP AMP DEsigned Values.

| FET | $\mathrm{W} / \mathrm{L}(\mu \mathrm{m} / \mu \mathrm{m})$ | FET | $\mathrm{W} / \mathrm{L}(\mu \mathrm{m} / \mu \mathrm{m})$ |
| :---: | :---: | :---: | :---: |
| $\mathrm{M}_{1}$ | $15 / 2.5$ | $\mathrm{M}_{6}, \mathrm{M}_{7}$ | $2000 / 2.5$ |
| $\mathrm{M}_{2}$ | $30 / 2.5$ | $\mathrm{M} 8, \mathrm{M}_{15}$ | $92 / 2.5$ |
| $\mathrm{M}_{3}$ | $50 / 4$ | $\mathrm{M}_{9}, \mathrm{M}_{14}$ | $1055 / 2.5$ |
| $\mathrm{M}_{4}$ | $44 / 6$ | $\mathrm{M}_{10}, \mathrm{M}_{13}$ | $2000 / 2.5$ |
| M 5 | $187 / 2.5$ | $\mathrm{M}_{11}, \mathrm{M}_{12}$ | $390 / 2.5$ |

consumption. When the power supply voltage is simply reduced, the gain of OP Amps is restrained and their bandwidths become low. So, in the newly developed circuit, each FET (Field Effect Transistor) size of the LV DSBFC OP Amp was optimized to achieve high-speed switching operation of 14.3 MHz . This OP Amp has a DSB circuit suitable for low power dissipation and an FC OP Amp to achieve a wide dynamic range even in low power supply voltages. The DSB circuit consists of a bias circuit of $\mathrm{M}_{1}-\mathrm{M}_{4}$ The FC OP Amp consists of a current mirror of M10-M13 and current sources of M8, M9, M14, and M15. The current sources $\mathrm{M}_{5}, \mathrm{M}_{8}$, and $\mathrm{M}_{15}$ of the FC OP Amp are controlled by switching a bias voltage $V_{\mathrm{B}}$ of the DSB circuit dynamically from $V_{\mathrm{B}} *$ to -1.5 V to reduce the power consumption still more. Table I shows its designed values. A minimum channel length of p-MOS FETs and n-MOS FETs is $2.5 \mu \mathrm{~m}$. In order to achieve almost the same transconductance $\mathrm{g}_{\mathrm{m}}$ as that in the conventional $5-\mathrm{V}$ power DSBFC OP Amp, a channel width W of $\mathrm{M}_{11}$ and $\mathrm{M}_{12}$ and that of $\mathrm{M}_{10}$ and $\mathrm{M}_{13}$, in p-MOS current mirror circuits, were increased by nearly fourfold and twofold, respectively. Each W of n-MOS current sources M9, M14, M8, and M15 was increased by nearly one and a half. The bias voltage of $V_{\mathrm{B}}{ }^{*}$ at the on state of the FC OP Amp was adjusted to nearly 0 V (larger than the conventional one) to decrease W of the current source M5 maintaining a high switching speed of the DSB circuit. W of $\mathrm{M}_{1}-\mathrm{M}_{3}$ was increased by over twofold. W of M4 was adjusted to an optimum value. The bias voltage Vb of the current source consisting of $\mathrm{M}_{9}$ and $\mathrm{M}_{14}$ was set at 0.15 V .

In the DSB circuit, when an external control pulse $\phi_{\mathrm{B}}$
driving an inverting switching circuit of $\mathrm{M}_{1}-\mathrm{M}_{4}$ is -1.5 V , the OP Amp turns on by setting $V_{\mathrm{B}}$ at an appropriate level of nearly 0 V by enabling $\mathrm{M}_{3}$ and $\mathrm{M}_{4}$ to operate in the saturation region, and operates normally as an operational amplifier. Conversely, when $\phi_{\mathrm{B}}$ becomes 1.5 V , the OP Amp turns off by setting $V_{\mathrm{B}}$ at nearly -1.5 V , enabling $\mathrm{M}_{1}$ to operate in a low impedance and $\mathrm{M}_{3}$ in a high impedance. This high impedance status of $\mathrm{M}_{3}$ occurs because the gate of $\mathrm{M}_{3}$ is set at a potential determined by the capacitive coupling between gate and source of $\mathrm{M}_{2}$ and between gate and drain of $\mathrm{M}_{3}$ at the transition of $\phi_{\mathrm{B}}$ to 1.5 V . Therefore, the OP Amp does not dissipate power at all during this off period, which brings about low power consumption.

## III. Simulation Results

The LV DSBFC OP Amp performance was tested through SPICE simulations. The power supply voltages $\mathrm{V}_{\mathrm{DD}}$ and Vss are 1.5 V . Typical performances compared with those of the conventional DSBFC OP Amp with a power supply of 5 V are shown in Table II. The values of parameters of open loop gain, phase margin, unity gain frequency, slew rate, and settling time are almost the same as those in the conventional $5-\mathrm{V}$ power DSBFC OP Amp. As the inherent static nonlinearity of the LV DSBFC OP Amp, the total harmonic distortion THD for the 10 kHz input signal, enabling $0.6 \mathrm{Vp}-\mathrm{p}$ to output, was $0.73 \%$, which is a little large compared to the conventional one. However, this is less than $1 \%$.

The LV DSBFC OP Amp operated in a dynamic switching mode with a Duty Ratio (DR) of $50 \%$ and a switching frequency, $f s$, of 14.3 MHz as shown in Figure 2. The output sine wave voltage for the input signal of 1 mV was nearly equal to that in the static operation mode of this OP Amp. Like this, the distortion by the dynamic operation seems to be hardly seen. In the dynamic switching operation mode of $50 \%$ duty ratio, the power dissipation was 9.3 mW , which is $66 \%$ of that $(14.0 \mathrm{~mW})$ observed in the static operation mode as shown in Figure 3. This is also 57 \% of that (16.3 mW ) of the conventional 5-V power DSBFC OP Amp. This shows this OP Amp's extremely low power consumption characteristics due to the reduced effect of power supply voltages ( $60 \%$ of that in the conventional $5-\mathrm{V}$ power

TABLE II. TYpical Performances for the Low-Voltage 3-V POWER AND CONVENTIONAL 5-V POWER DSBFC OP AMPS. $\mathrm{C}_{\mathrm{L}}=1 \mathrm{PF}$.

| Performance parameters | 3 V power DSBFC OP <br> Amp - this work | 5 V power DSBFC OP <br> Amp |
| :--- | :---: | :---: |
| Power supply voltages | $\pm 1.5 \mathrm{~V}$ | $\pm 2.5 \mathrm{~V}$ |
| Switching frequency $f s$ | 14.3 MHz | 14.3 MHz |
| Open loop gain Ao | 47.1 dB | 51 dB |
| Phase margin $\theta$ | 32.8 degrees | 34.2 degrees |
| Unity gain frequency $f u$ | 603.7 MHz | 709 MHz |
| Slew rate SR (CL $=10 \mathrm{pF})$ | $131 \mathrm{~V} / \mu \mathrm{s}$ | $140 \mathrm{~V} / \mu \mathrm{s}$ |
| Settling time ts | 10 ns | 12 ns |
| Distortion THD <br> (fin $=10 \mathrm{kHz}, ~ V o=0.6 \mathrm{Vp}-\mathrm{p})$ | $0.73 \%$ | $0.40 \%$ |
| Power dissipation $\left(\mathrm{C}_{\mathrm{L}}=5 \mathrm{pF}\right)$ <br> in $50 \%$ switching duty ratio | 9.3 mW | 16.3 mW |



Figure 2. Simulation waveforms of the low-voltage DSBFC OP Amp. Input signal frequency $f_{i n}=1 \mathrm{MHz}, V_{i n}=1 \mathrm{mV}, f_{s}=14.3 \mathrm{MHz}, \mathrm{C}_{\mathrm{L}}=2 \mathrm{pF}$.


Figure 3. Power dissipation vs. OP-Amp switching duty ratio in the DSB mode. $f_{s}=14.3 \mathrm{MHz}, \mathrm{C}_{\mathrm{L}}=5 \mathrm{pF}$.


Figure 4. Dynamic offset voltage vs. OP Amp load capacitance in the LV DSBFC OP Amp. $f_{i n}=0.5 \mathrm{MHz}, V_{i n}=1 \mathrm{mV}$.

DSBFC OP Amp) and dynamic switching operation.
The LV DSBFC OP Amp switches dynamically to the off state. At this time, though p-MOSFETs M11 and M12
remain the on-state, MOSFETs $\mathrm{M}_{6}$, $\mathrm{M}_{7}$, $\mathrm{M}_{9}$, $\mathrm{M}_{10}$, $\mathrm{M}_{13}$, and M14 change to the on-state weakly. The output terminal of Vo of the OP Amp is set at a voltage depending on the load capacitance through the capacitive coupling between the drain and the gate of the MOSFET M13. So, a large output swing in $V o$ occurs at the off-state transition. A dynamic offset voltage Voff (defined as the difference of the on-state and the off-state output voltages) at the off-state transition of the OP Amp vs. load capacitance $C_{L}$ was tested (Figure 4). In small load capacitances less than 1.5 pF , top and bottom signal levels of the dynamic off swing do not match. This causes distortion at an output signal of the OP Amp. Therefore, we can see that the load capacitance $C_{L}$ over 2 pF is desirable for its operation.

## IV. ApPLICATION TO SC LPFs

To demonstrate the practicability of the above LV DSBFC OP Amp, the feasibility of its application to two kinds of SC LPFs was investigated.

## A. $2^{\text {nd }}$-Order SC LPF

At first, a $2^{\text {nd }}$-order SC IIR (Infinite Impulse Response) LPF with the Butterworth frequency characteristic was tested. When a sampling frequency $f \mathrm{~s}=14.3 \mathrm{MHz}$ (equal to four times of NTSC (National Television System Committee) color sub-carrier frequency 3.58 MHz ) and a cutoff frequency $f_{c}=2 \mathrm{MHz}$, respectively, were chosen for this LPF, the discrete-time transfer function using the z-transform is given by (1) [11].

$$
\begin{equation*}
\mathrm{H}_{1}(\mathrm{z})=-\frac{0.11735\left(1+\mathrm{z}^{-1}\right)^{2}}{1-0.82524 \mathrm{z}^{-1}+0.29464 \mathrm{z}^{-2}} \tag{1}
\end{equation*}
$$

The circuit configuration and operation waveforms realizing this transfer function are shown in Figures 5 and 6, respectively [11]. This SC LPF was designed referencing an SC biquadratic circuit with integrators in the reference [12]. It consists of a sample-hold circuit with a holding capacitor Cs1 and a CMOS sampling switch controlled by $\phi_{\mathrm{SH}}$, CMOS switches $\phi_{1}, \phi_{2}$ for charge transfer, capacitors A-E, G, and I, and two LV DSBFC OP Amps (OP Amps 1 and 2). In this SC LPF, in order to enable easily to determine the capacitance value of each capacitor, the coefficient of A is set to be equal to that of B. Capacitors in this SC LPF can be basically divided into two groups. In one group (C, D, E, and


Figure 5. Configuration of the $2^{\text {nd }}$-order SC LPF.


Figure 6. Operation waveforms of the $2^{\text {nd }}$-order SC LPF.
G ), charges are supplied to OP Amp 1. In another group (A, B, and I), charges are supplied to OP Amp 2. Even if a capacitance of each capacitor group is multiplied by constant times, the transfer function of the SC LPF does not change because the multiplication of two capacitor coefficients is performed in the numerator and the denominator of its transfer function, respectively. Therefore, capacitances of integral capacitors B and D are here chosen as a reference capacitance in each group and each coefficient of $B$ and $D$ is normalized to 1 . At this time, 1 for every normalized coefficient of $A, B$, and $D$ is obtained because $A$ and $B$ were set to the same coefficient as described above. In Figure 5, when the coefficients of $\mathrm{A}, \mathrm{B}$, and D are normalized to 1 , other coefficients are determined in the following.

$$
\begin{aligned}
& \mathrm{I}=\mathrm{K}=0.11735 \\
& \mathrm{G}=2 \mathrm{~K}+2 \mathrm{I}=0.4694 \\
& \mathrm{C}=1+\mathrm{b}_{1}+\mathrm{b}_{2}=0.4694 \\
& \mathrm{E}=1-\mathrm{b}_{2}=0.70536
\end{aligned}
$$

Here, $b_{1}=-0.82524$ and $b_{2}=0.29464$. When the smallest coefficient of $\mathrm{I}(=0.11735)$ is replaced as a reference capacitance of 0.5 pF , each capacitance in the SC LPF IC is set in proportion to the above coefficient as shown in Figure 5.

Because an SC LPF's input signal is desirable to be maintained by a sample-hold circuit for stabilizing, this sample-hold circuit is applied to the SC LPF. In this case, the transfer function is multiplied by the following zero-order hold function due to a sample-hold effect.

$$
\begin{equation*}
H_{s}(j \omega)=\frac{\sin \left(\omega T_{s} / 2\right)}{\omega T_{s} / 2} \tag{2}
\end{equation*}
$$

Here, Ts represents the one cycle period of sampling pulses. Therefore, when the transfer function (1) is replaced using $\mathrm{z}=\mathrm{e}^{j \omega T_{\mathrm{s}}}$, the magnitude of the transfer function of the $2^{\text {nd }}$ order SC LPF considering the sample-hold effect is given by (3).

$$
\begin{equation*}
|H(j \omega)|=\frac{\sin \left(\omega \mathrm{T}_{\mathrm{s}} / 2\right)}{\omega \mathrm{T}_{\mathrm{s}} / 2}\left|\mathrm{H}_{1}(j \omega)\right| \tag{3}
\end{equation*}
$$

Here, $\left|\mathrm{H}_{1}(j \omega)\right|$ in (3) is the following function.

$$
\begin{equation*}
\left|\mathrm{H}_{1}(j \omega)\right|=\frac{0.2347\left(1+\cos \left(\omega \mathrm{T}_{\mathrm{s}}\right)\right)}{\sqrt{1.76783-2.13678 \cos \left(\omega \mathrm{~T}_{\mathrm{s}}\right)+1.65128 \cos \left(2 \omega \mathrm{~T}_{\mathrm{s}}\right)}} \tag{4}
\end{equation*}
$$

The sampling switch was designed to a channel width / channel length $\mathrm{W} / \mathrm{L}=105 / 2.5(\mu \mathrm{~m} / \mu \mathrm{m})$ for each of p MOSFET and n-MOSFET. Other CMOS switches were designed to $75 / 2.5(\mu \mathrm{~m} / \mu \mathrm{m})$. CMOS switches are turned on and off by non-overlapping two-phase clock pulses $\phi_{1}, \phi_{2}$, swinging from -1.5 V to 1.5 V . These sampling and CMOS switches were designed to have a balanced structure with each equal $L$ and $W$ of p-MOS and n-MOS FETs to suppress a feed-through phenomenon as much as possible. This phenomenon is easy to be caused by a capacitive coupling between gate and output terminals.

Major CMOS process parameters are given as a gate insulating film thickness $\mathrm{t}_{\mathrm{ox}}=50 \mathrm{~nm}$, a p-MOSFET threshold voltage $\mathrm{V}_{\mathrm{TP}}=-0.6 \mathrm{~V}$, and an n -MOSFET threshold voltage $\mathrm{V}_{\mathrm{Tn}}=0.6 \mathrm{~V}$.

The operation principle of this SC LPF is as follows. The output signal $V_{01}$ of OP Amp 1 is obtained as an additional output of an integrated signal of $V$ in using a negative integrator (capacitor D, G SC circuit, and OP Amp 1), an integrated signal of Vout using a negative integrator (capacitor D, C SC circuit, and OP Amp1), and a signal multiplied $V_{\text {out }}$ by E/D. The output signal $V_{\text {out }}$ is an additional output of an integrated signal of $V_{\mathrm{ol}}$ using a positive integrator (A SC circuit, capacitor B, and OP Amp 2), and a signal multiplied $V$ in by I/B. Vout is basically fed back to an input of OP Amp 1 like this. $V$ in is also integrated twice and added after being decreased by an appropriate capacitance ratio. Due to these integration using positive and negative integrators, addition and feedback operations, the function of LPF is achieved.

The actual operation of the SC LPF is described in the following. In this SC LPF, charge transfer operations through clock pulses $\phi_{1}, \phi_{2}$, are performed during the on-state period To of the LV DSBFC OP Amps (when the control pulse $\phi_{\mathrm{B}}$ is set at -1.5 V ). The off-state period $\mathrm{T}_{\mathrm{B}}$ (the remaining period of the one cycle period Ts) is separately provided to realize low power consumption for this SC LPF. An input signal $V_{\mathrm{in}}$ is sampled during the sampling phase of $\phi_{\mathrm{SH}}(10$ ns) in the on-state period To. After sampling operation, its corresponding charge is stored on the holding capacitor Cs1. The voltage at the off-state transition of $\phi_{\mathrm{SH}}$ is transferred to an output terminal $V_{\text {out, charging all capacitors, during the }}$ clock phase of $\phi_{1}$. During the subsequent clock phase of $\phi_{2}$, each charge of two capacitors C and G is discharged and each charge of remaining capacitors is redistributed. During such on-state period of To, the LV DSBFC OP Amps turn on by setting a bias voltage of $V_{\mathrm{B}}$ at an appropriate level of nearly 0 V and operate normally as operational amplifiers.

Subsequently, $\phi_{\mathrm{B}}$ becomes 1.5 V at the off-state transition of the OP Amps, while $\phi_{2}$ is switched off. During this off period $T_{B}$, the OP Amps turn off and so these do not dissipate power at all. Therefore, when $T_{B}$ is set relatively long as compared to the one-cycle period Ts , the power


Figure 7. Simulation waveforms for the $2^{\text {nd }}$-order SC LPF. $V_{i n}=0.3 V_{0}-p$, $f_{\text {in }}=1 \mathrm{MHz}, \mathrm{C}_{\mathrm{L}}=4 \mathrm{pF}$.


Figure 8. Frequency response of the $2^{\text {nd }}$-order SC LPF in the DSB mode of the OP Amp. $\mathrm{T}_{\mathrm{B}}=35 \mathrm{~ns}$.
consumption of the SC LPF is expected to become lower than that observed in ordinary static operation for an SC LPF using conventional OP Amps.

Operation waveforms for an input signal of 1 MHz with an amplitude of 0.3 V and an output load of 4 pF are shown in Figure 7. In the dynamic switching operation, an output load of the LV DSBFC OP Amp increases to nearly 5 pF including internal capacitances of the SC LPF. For the passband frequency signal ( $\leqq 2 \mathrm{MHz}$ ), almost the same signal as the input one was obtained. The frequency response of the SC LPF in the dynamic switching operation of the LV DSBFC OP Amp is shown in Figure 8. Figure 9 shows the frequency response of the SC LPF in the static operation mode of OP Amps. Both frequency responses are almost the same. This means that there is almost no gain deterioration by employing the DSB operation of the LV DSBFC OP Amps. The frequency response was near the theoretical one from 100 kHz to near 5 MHz . In the high frequency range over 6 MHz , it deteriorated due to a sampling phase effect. The gain below -26 dB was obtained at over 6 MHz within the stop-band. Though this stop-band gain is not low enough, it is expected to be improved by making the roll-off steeper through the increase of filter order.


Figure 9. Frequency response of the $2^{\text {nd }}$-order SC LPF in the static operation mode of the OP Amp. $\phi_{\mathrm{B}}=-1.5 \mathrm{~V}$.


Figure 10. Power dissipation vs. OP Amp switching duty ratio in the $2^{\text {nd }}-$ order SC LPFs. $f_{i n}=1 \mathrm{MHz}$.

The power dissipation vs. the OP Amp switching duty ratio in the $2^{\text {nd }}$-order SC LPF is shown in Figure 10. The power dissipation of the SC LPF itself decreased in proportion to the off period $\mathrm{T}_{\mathrm{B}}$ of the OP Amp. In the dynamic switching operation mode of $\mathrm{T}_{\mathrm{B}}=35 \mathrm{~ns}(\mathrm{DR}=50 \%)$, the power dissipation of the SC LPF $(18.7 \mathrm{~mW})$ was reduced to $66.8 \%$ as compared to that in the static operation of the OP Amps ( 28.0 mW ). Thus, the dynamic switching operation of the LV DSBFC OP Amp is useful for reducing the power dissipation of the SC LPF. This power dissipation was $56.8 \%$ compared to that in the SC LPF using the conventional 5-V power DSBFC OP Amp ( 32.9 mW ). This low power characteristic was realized by the low power supply voltages and dynamic switching operation.

## B. $4^{\text {th }}$-Order $S C L P F$

As another application example of the above LV DSBFC OP Amp, a $4^{\text {th }}$-order SC IIR LPF with the Butterworth frequency characteristic was tested. The high filter order of the fourth was selected because it is expected to achieve a sharp roll-off gain characteristic. The $4^{\text {th }}$-order SC LPF was designed to achieve a roll-off characteristic with a gain of below -30 dB at over 4 MHz within the stop-band. The other design condition was set as follows. That is, the sampling frequency $f \mathrm{~s}=14.3 \mathrm{MHz}$ and the cutoff frequency $f \mathrm{c}=2 \mathrm{MHz}$ were chosen as the same values as those in the $2^{\text {nd }}$-order SC LPF, that enables it to process video signals. Under this condition, the discrete-time transfer function is given using the z-transform by (5). That is, (5) can be rewritten like (6) considering the independence of two transfer functions.

$$
\begin{equation*}
\mathrm{H}_{2}(\mathrm{z})=\frac{-0.10573\left(1+\mathrm{z}^{-1}\right)^{2}}{1-0.74578 \mathrm{z}^{-1}+0.16869 \mathrm{z}^{-2}} \cdot \frac{-0.13976\left(1+\mathrm{z}^{-1}\right)^{2}}{1-0.98582 \mathrm{z}^{-1}+0.54484 \mathrm{z}^{-2}} \tag{5}
\end{equation*}
$$

$$
\begin{equation*}
\mathrm{H}_{2}(\mathrm{z})=\mathrm{H}_{21}(\mathrm{z}) \cdot \mathrm{H}_{22}(\mathrm{z}) \tag{6}
\end{equation*}
$$

The circuit configuration realizing this transfer function is shown in Figure 11 [13]. Its operation waveforms are the same as those in the $2^{\text {nd }}$-order SC LPF shown in Figure 6. The $4^{\text {th }}$-order SC LPF was designed referencing a SC biquadratic circuit with integrators [12] in the same way as the $2^{\text {nd }}$-order SC LPF. This SC LPF consists of two-stage biquadratic circuits cascading two $2^{\text {nd }}$-order SC LPFs of LPF1 and LPF2, provided with a sample-hold circuit with a holding capacitor Cs 1 and a sampling switch controlled by $\phi_{\mathrm{SH}}, \mathrm{CMOS}$ switches $\phi_{1}$ and $\phi_{2}$, capacitors $\mathrm{A}_{1}, \mathrm{~B}_{1}, \mathrm{C}_{1}, \mathrm{D}_{1}$, $E_{1}, G_{1}, I_{1}, A_{2}, B_{2}, C_{2}, D_{2}, E_{2}, G_{2}$, and $I_{2}$, and four LV DSBFC OP Amps. The transfer function of this SC LPF circuit is shown in (7).

$$
\begin{align*}
\mathrm{H}_{2}(\mathrm{z})= & (-) \frac{\mathrm{D}_{1} \mathrm{I}_{1}+\left(\mathrm{A}_{1} \mathrm{G}_{1}-2 \mathrm{D}_{1} \mathrm{I}_{1}\right) \mathrm{z}^{-1}+\mathrm{D}_{1} \mathrm{I}_{1} \mathrm{z}^{-2}}{\mathrm{D}_{1} \mathrm{~B}_{1}+\left(\mathrm{A}_{1} \mathrm{C}_{1}+\mathrm{A}_{1} \mathrm{E}_{1}-2 \mathrm{D}_{1} \mathrm{~B}_{1}\right) \mathrm{z}^{-1}+\left(\mathrm{D}_{1} \mathrm{~B}_{1}-\mathrm{A}_{1} \mathrm{E}_{1}\right) \mathrm{z}^{-2}} \\
& \cdot(-) \frac{\mathrm{D}_{2} \mathrm{I}_{2}+\left(\mathrm{A}_{2} \mathrm{G}_{2}-2 \mathrm{D}_{2} \mathrm{I}_{2}\right) \mathrm{z}^{-1}+\mathrm{D}_{2} \mathrm{I}_{2} \mathrm{z}^{-2}}{\mathrm{D}_{2} \mathrm{~B}_{2}+\left(\mathrm{A}_{2} \mathrm{C}_{2}+\mathrm{A}_{2} \mathrm{E}_{2}-2 \mathrm{D}_{2} \mathrm{~B}_{2}\right) \mathrm{z}^{-1}+\left(\mathrm{D}_{2} \mathrm{~B}_{2}-\mathrm{A}_{2} \mathrm{E}_{2}\right) \mathrm{z}^{-2}} \tag{7}
\end{align*}
$$

The same way of thinking as that in the $2^{\text {nd }}$-order SC LPF is applicable in determining each capacitance of LPF1 ( $\mathrm{A}_{1}$, $B_{1}, C_{1}, D_{1}, E_{1}, G_{1}$, and $\left.I_{1}\right)$ and $\operatorname{LPF} 2\left(A_{2}, B_{2}, C_{2}, D_{2}, E_{2}, G_{2}\right.$, and $\mathrm{I}_{2}$ ) as well. As shown in (5) and (6), each transfer function for the LPF1 and LPF2 is independent of each other. Therefore, the normalization of the coefficients in the LPF1 and LPF2 can be made independently. In Figure 11, when the coefficients of $\mathrm{A}_{1}, \mathrm{~B}_{1}, \mathrm{D}_{1}, \mathrm{~A}_{2}, \mathrm{~B}_{2}$, and $\mathrm{D}_{2}$ are normalized to 1 , the transfer function (7) is changed to (8).

$$
\begin{align*}
\mathrm{H}_{2}(\mathrm{z})= & (-) \frac{\mathrm{I}_{1}+\left(\mathrm{G}_{1}-2 \mathrm{I}_{1}\right) \mathrm{z}^{-1}+\mathrm{I}_{1} \mathrm{z}^{-2}}{1+\left(\mathrm{C}_{1}+\mathrm{E}_{1}-2\right) \mathrm{z}^{-1}+\left(1-\mathrm{E}_{1}\right) \mathrm{z}^{-2}} \\
& \cdot(-) \frac{\mathrm{I}_{2}+\left(\mathrm{G}_{2}-2 \mathrm{I}_{2}\right) \mathrm{z}^{-1}+\mathrm{I}_{2} \mathrm{z}^{-2}}{1+\left(\mathrm{C}_{2}+\mathrm{E}_{2}-2\right) \mathrm{z}^{-1}+\left(1-\mathrm{E}_{2}\right) \mathrm{z}^{-2}} \tag{8}
\end{align*}
$$



Figure 11. Configuration of the $4^{\text {th }}$-order SC LPF.

Because the coefficients in (8) are equal to those in (5), other coefficients are determined as follows.

$$
\begin{aligned}
& \mathrm{I}_{1}=\mathrm{K}_{1}=0.10573 \\
& \mathrm{G}_{1}=4 \mathrm{~K}_{1}=0.42292 \\
& \mathrm{C}_{1}=1+\mathrm{b}_{11}+\mathrm{b}_{12}=0.42291 \\
& \mathrm{E}_{1}=1-\mathrm{b}_{12}=0.83131 \\
& \mathrm{I}_{2}=\mathrm{K}_{2}=0.13976 \\
& \mathrm{G}_{2}=4 \mathrm{~K}_{2}=0.55904 \\
& \mathrm{C}_{2}=1+\mathrm{b}_{21}+\mathrm{b}_{22}=0.55902 \\
& \mathrm{E}_{2}=1-\mathrm{b}_{22}=0.45516
\end{aligned}
$$

Here, $\mathrm{b}_{11}=-0.74578, \mathrm{~b}_{12}=0.16869, \mathrm{~b}_{21}=-0.98582$, and $\mathrm{b}_{22}=0.54484$. When the smallest coefficients of $\mathrm{I}_{1}=0.10573$ in the LPF1 and $\mathrm{I}_{2}=0.13976$ in the LPF2 are replaced as a reference capacitance of 0.5 pF , each capacitance in the $4^{\text {th }}$ order SC LPF IC is set in proportion to the above coefficients as shown in Figure 11. A sample-hold circuit is also applied in this SC LPF to maintain its input signal for stabilizing. At this time, the transfer function (5) is multiplied by the zero-order hold function (2) in the same way as that in the previous $2^{\text {nd }}$-order SC LPF. Therefore, when the transfer function (5) or (6) is replaced using $\mathrm{z}=\mathrm{e}^{j \omega \mathrm{~T}_{\mathrm{s}}}$, the magnitude of the transfer function of the $4^{\text {th }}$ order SC LPF considering the sample-hold effect is given by


Figure 12. Gain vs. channel width of sampling switch MOSFETs. Cs $1=1 \mathrm{pF}$.


Figure 13. Gain vs. holding capacitance. W/L of sampling switch MOSFETs=140/2.5 ( $\mu \mathrm{m} / \mu \mathrm{m}$ ).
(9).

$$
\begin{equation*}
|H(j \omega)|=\frac{\sin \left(\omega \mathrm{T}_{\mathrm{s}} / 2\right)}{\omega \mathrm{T}_{\mathrm{s}} / 2}\left|\mathrm{H}_{21}(j \omega)\right| \cdot\left|\mathrm{H}_{22}(j \omega)\right| \tag{9}
\end{equation*}
$$

Here, $\left|\mathrm{H}_{21}(j \omega)\right|$ and $\left|\mathrm{H}_{22}(j \omega)\right|$ in (9) are the following functions, respectively.

$$
\begin{align*}
\left|\mathrm{H}_{21}(j \omega)\right| & =\frac{0.21146\left(1+\cos \left(\omega \mathrm{T}_{\mathrm{s}}\right)\right)}{\sqrt{1.58464-1.74317 \cos \left(\omega \mathrm{~T}_{\mathrm{s}}\right)+0.33738 \cos \left(2 \omega \mathrm{~T}_{\mathrm{s}}\right)}}  \tag{10}\\
\left|\mathrm{H}_{22}(j \omega)\right| & =\frac{0.27953\left(1+\cos \left(\omega \mathrm{T}_{\mathrm{s}}\right)\right)}{\sqrt{2.26869-3.04587 \cos \left(\omega \mathrm{~T}_{\mathrm{s}}\right)+1.08968 \cos \left(2 \omega \mathrm{~T}_{\mathrm{s}}\right)}} \tag{11}
\end{align*}
$$

In this $4^{\text {th }}$-order SC LPF, the load capacitances of LV DSBFC OP Amps were set as a 2 pF because twofold capacitances as compared to that in the $2^{\text {nd }}$-order SC LPF are loaded. The sample-hold circuit in this SC LPF was designed


Figure 14. Simulation waveforms for the $4^{\text {th }}$-order SC LPF. $V_{\text {in }}=0.3 V_{0}$-p, $f_{i n}=1 \mathrm{MHz}, \mathrm{C}_{\mathrm{L}}=2 \mathrm{pF}$.
as follows considering the feed-through phenomenon.
Figure 12 shows the gain of the $4^{\text {th }}$-order SC LPF in the DSB mode of the LV DSBFC OP Amp vs. the channel width Wsh of each of p-MOSFET and n-MOSFET in the sampling switch. The gain of the $4^{\text {th }}$-order SC LPF became minimum at a $W_{\text {sh }}$ of nearly $140 \mu \mathrm{~m}$ when the input signal frequency $f$ in is equal to 5 MHz within the stop-band, while its gain remains almost unchanged for input signals of 1 and 2 MHz within the passband. This is thought to be due to the following phenomenon. When Wsh is larger than $140 \mu \mathrm{~m}$, the feed-through via the difference of capacitive coupling between gate and output terminals of the above MOSFETs does not become negligible at the off-state transition of the sampling switch and so the gain corresponding to $f \mathrm{in}=5 \mathrm{MHz}$ increases. When Wsh is smaller than this value, a driving ability of the sampling switch becomes insufficient, which brings about an increase of the gain. Like this, Wsh of the sampling switch is optimized to $140 \mu \mathrm{~m}$. The feed-through in the sample-hold circuit is also dependent on a holding capacitance. Figure 13 shows the gain of the $4^{\text {th }}$-order SC LPF in the DSB mode of the LV DSBFC OP Amp vs. the holding capacitance. As the holding capacitance Cs1 increases, the gain corresponding to $f \mathrm{in}=5 \mathrm{MHz}$ in the stopband deteriorates little by little. That is, we can see that a smaller capacitance is desirable as Csı. So, the Cs1 of 1 pF in this $4^{\text {th }}$-order SC LPF was also chosen.

Other CMOS switches were designed to $75 / 2.5(\mu \mathrm{~m} / \mu \mathrm{m})$, which is the same one as that in the $2^{\text {nd }}$-order SC LPF. In this $4^{\text {th }}$-order SC LPF consisting of a cascade connection of two different $2^{\text {nd }}$-order SC LPFs of LPF1 and LPF2 and a sample-hold circuit for common use, the operation principle is similar to the previous $2^{\text {nd }}$-order SC LPF

Operation waveforms for an input signal of 1 MHz with an amplitude of 0.3 V and an output load of 2 pF are shown in Figure 14. In the $4^{\text {th }}$-order SC LPF, the output signal amplitude nearly close to the input signal was also obtained for passband frequency signals. The frequency response of the $4^{\text {th }}$-order SC LPF in the dynamic switching operation of the LV DSBFC OP Amps is shown in Figure 15. The roll-off characteristic in near 3-4 MHz was greatly improved compared to that in the $2^{\text {nd }}$-order SC LPF. The response was near the theoretical one from 100 kHz up to near 4 MHz . At 4 MHz within the stop-band, the gain below -28 dB was obtained. In the high frequency range over 5 MHz within the stop-band, although it deteriorated due to a sampling phase


Figure 15. Frequency response of the $4^{\text {th }}$-order SC LPF in the DSB mode of the LV DSBFC OP Amp. $\mathrm{T}_{\mathrm{B}}=35 \mathrm{~ns}$.


Figure 16. Power dissipation vs. OP Amp switching duty ratio in the $4^{\text {th }}-$ order SC LPFs. $f_{i n}=1 \mathrm{MHz}$.
effect, the gain below -31.5 dB (a practical level) was achieved. In this way, a wide stop-band with a high attenuation (a sharp roll-off characteristic) in the high frequency response became possible due to the two-stage biquadratic SC LPF configuration with the increased filter order of the fourth. Like this, it is clear that the LV DSBFC OP Amp is also applicable to the high-order SC LPF.

The power dissipation vs. the OP-Amp switching duty ratio in the $4^{\text {th }}$-order SC LPF with the $3-V$ power LV DSBFC OP Amps compared to that in the $4^{\text {th }}$-order one with conventional $5-\mathrm{V}$ power DSBFC OP Amps is shown in Figure 16. The power dissipation of the $4^{\text {th }}$-order SC LPF with the LV DSBFC OP Amps itself decreased in proportion to the off-state period $T_{B}$ of the OP Amps. In the dynamic switching operation mode of $\mathrm{T}_{\mathrm{B}}=35 \mathrm{~ns}(=50 \%$ switching duty ratio) and $\phi_{1}=\phi_{2}=15 \mathrm{~ns}$, the power consumption of this $4^{\text {th }}$-order SC LPF $(37.4 \mathrm{~mW})$ decreased to $66.8 \%$ as

TABLE III. TYPICAL PERFORMANCES FOR THE $2^{\text {ND }}$-ORDER AND $4^{\text {TH }}$ ORDER SC LPFs EMPLOYING THE LV DSBFC OP AMPS.

| Performance parameters | Simulation results |  |
| :---: | :---: | :---: |
|  | 4th-order SC LPF | 2nd-order SC LPF |
| Sampling and switching frequency $f$ s | 14.3 M Hz | 14.3 M Hz |
| Input signal amplitude | 0.3 V0-P | 0.3 V0-P |
| Cutoff frequency $f \mathrm{c}$ | 2 MHz | 2 MHz |
| Gain at a stop-band over 5 MHz | $\leqq-31.5 \mathrm{~dB}$ (Dynamic mode) | $\leqq-26.0 \mathrm{~dB}$ (Dynamic mode) |
| Power consumption | 56.0 mW (Static) | 28.0 mW (Static) |
|  | $\begin{gathered} 37.4 \mathrm{~mW} \\ \text { (Dy namic: } \mathrm{T}_{\mathrm{B}} / \mathrm{Ts}_{\mathrm{s}}=50 \% \text { ) } \end{gathered}$ | $\begin{gathered} 18.7 \mathrm{~mW} \\ (\text { Dy namic: } \mathrm{T} / \mathrm{T} \mathrm{~T}=50 \% \text { ) } \end{gathered}$ |

compared to that in the static operation of the LV DSBFC OP Amps ( 56 mW ). This value is twice as large as that in the $2^{\text {nd }}$-order SC LPF with the LV DSBFC OP Amps ( 18.7 mW ) because the $4^{\text {th }}$-order SC LPF consists of a cascadeconnection of two $2^{\text {nd }}$-order SC LPFs. However, the power consumption of this $4^{\text {th }}$-order SC LPF with the LV DSBFC OP Amps at $50 \%$ switching duty ratio was reduced to 56.9 \% compared to that in the $4^{\text {th }}$-order SC LPF with conventional 5-V power DSBFC OP Amps ( 65.7 mW ). Thus, even when the DSBFC OP Amps are applied to the twostage biquadratic circuits of SC LPF, the dynamic operation of these LV DSBFC OP Amps enabling low power consumption as compared to their static operation is also useful for reducing the power consumption of SC LPF. Typical characteristics of the $4^{\text {th }}$-order SC LPF compared with those of the $2^{\text {nd }}$-order SC LPF employing the LV DSBFC OP Amps are listed in Table III.

## V. CONCLUSIONS

A high-speed Low-Voltage (LV) Folded-Cascode (FC) Operational Amplifier (OP Amp) with a Dynamic Switching Bias (DSB) circuit capable of processing video signals, which enables low power consumption, high gain with wide bandwidths, and a wide dynamic range, was proposed. Through simulations, it was shown that the OP Amp with the reduced 3-V power supply is able to operate at a 14.3 MHz dynamic switching rate, allowing processing video signals, and a dissipated power of $57 \%$ compared to that in the conventional $5-\mathrm{V}$ power DSBFC OP Amp while keeping a 0.6 V wide output dynamic range. The response of the $2^{\text {nd }}-$ order Switched Capacitor Low-Pass Filter (SC LPF) tested as its application was near the theoretical frequency response within frequencies below 5 MHz . The power dissipation of this LPF was also reduced to $56.8 \%$ of that in the $2^{\text {nd }}-$ order SC LPF with conventional 5-V power DSBFC OP Amps. As another application of the LV DSBFC OP Amps, the $4^{\text {th }}$ order SC LPF was tested to achieve a practical sharp roll-off gain characteristic. The roll-off response of this $4^{\text {th }}$-order SC LPF was greatly improved compared to that in the $2^{\text {nd }}$-order SC LPF. At over 5 MHz within the stop-band, a practical level gain below -31.5 dB was achieved. The power consumption of this $4^{\text {th }}$-order SC LPF decreased to $56.9 \%$ of that in the $4^{\text {th }}$-order SC LPF with conventional $5-\mathrm{V}$ power DSBFC OP Amps.

Thus, it was confirmed that the $3-V$ power DSBFC OP

Amp is useful for high speed operation, low power consumption, and greatly reducing the power dissipation of the SC LPFs. This circuit should be useful for the realization of low-power wide-band signal processing ICs. For example, it has a possibility of changing current A/D (Analog-toDigital) converters, D/A (Digital-to-Analog) converters, and active-RC LPFs in CCD cameras into low-power SC circuits employing this LV DSBFC OP Amp, and of realizing lowpower SC versions instead of current SC Amps for prevention of the deterioration of CCD camera's output signal. It has also applicability to Amps and/or LPFs required in various kinds of sensing devices and video equipment. Furthermore, it is noteworthy that the performance is expected to be improved still more by employing MOSFETs with a minimum shorter channel length than $2.5 \mu \mathrm{~m}$ used in this work.

As shown above, although the frequency response was improved to a practical level by increasing the filter order, there might be a limitation in the filter order, because one OP Amp per one order LPF must be used and so power dissipation will increase in proportion to the filter order.

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