

# Towards a Decision Support System for Automated Selection of Optimal Neural Network Instance for Research and Engineering

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**Abstract**— The success of any advanced computing method (ACM) depends as much on its excellence as it does on a) whether it is optimally deployed and b) if it matches the problem at hand. Neural Networks, which are ACMs of remarkable potential, receive severe penalties in both of the latter aspects, due to reasons, put forth and addressed herein. This paper presents a theoretical foundation for an inference engine decision space and a taxonomic framework for a knowledge base, which are part of our proposed knowledge-driven decision support system (DSS) for optimal matching of a neural network (NN) setup against the given learning task. Such DSS supports solving a multiple criteria optimization problem, considering specific design constraints of the given NN-based machine learning application.

**Keywords** — *Neural Networks; Decision Support System; Knowledge base; Taxonomy; Multiple-Criteria Optimization Problem.*

## I. INTRODUCTION

The compelling notion, that NNs are universal approximators [1], leads quickly to believe, that any NN will do well on any presented machine learning task. However, the universal approximation theorem only guarantees the existence of an approximation, but not that it can be learned, nor that it would be efficient. Practice shows that every given problem requires a carefully crafted NN design and that advanced NN concepts, tailored to specific types of tasks are necessary to attain best results. This factor, among others, has led to the existence of a large number of conceptually varying NN architectures and learning algorithms [2].

For best results, any researcher or practitioner of today needs to understand a vast domain of knowledge in order to find a NN solution most suitable to their task. Due to domain vastness, researchers often limit themselves to NN domains they are familiar with, preventing new knowledge from propagating efficiently among all who would benefit from it. Specifically, we thus face a twofold handicap for progress of NN research: a) practitioners use suboptimal NN setups for real-world applications [2], inhibiting broader NN acceptance in the industry and b) researchers delve into local extrema of research (e.g., through jumping on the bandwagon of imminent peers [3]), pushing frontiers of NN research in suboptimal directions.

Figure 1 shows a simple flowchart view of the current typical approach to selection of NNs for chosen learning task. It can be seen, that the lack of systematic approach to NN selection often yields suboptimal results. This has a negative effect on a wider acceptance of NNs in the industry. A key prerequisite in current NN design is expert intuition, which can be attained either through significant experience with NN implementation and applications in practice, or through access to expert intuition in an environment of experienced NN users. When expert intuition is present in early stages of design, the subsequent efforts give good results (Figure 1, left); when not, design efforts too often lead to suboptimal results (Figure 1, right).

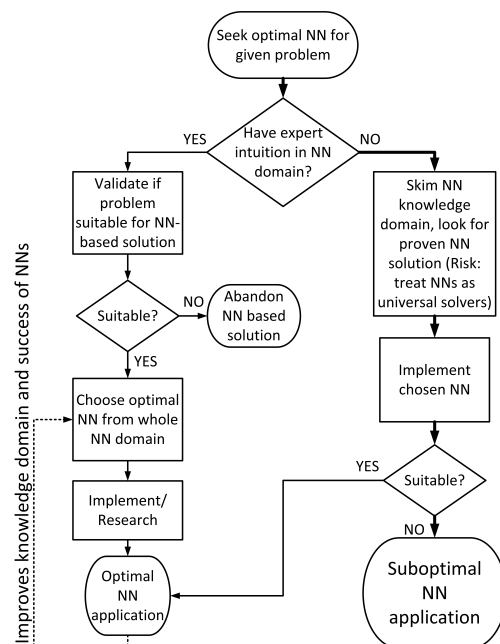


Figure 1. Typical design flow of selection and implementation of NNs for a given learning task.

The NN community needs a streamlined way of enabling existing and potential NN users to make optimal technological choices efficiently and systematically. Having today’s foremost

NN research applied in the industry can foster wider acceptance of NNs into practice and improve NN research. In 2006, Taylor and Smith [4] created an important taxonomy-based evaluation of NNs, which aids in validating whether a given problem is solvable with a NN at all. The next concern, which they point out and we hereby address, is to choose the right NN architecture and its concrete implementation for the problem. Our goal is to provide a decision support system (DSS) for industry practitioners and researchers to systematically find the right NN for their application or research interest. This paper proposes a solution that enables (1) a systematical overview of the complete NN knowledge domain to (2) compare NN instances through their capabilities in a (3) quickly interpretative way using a framework that is (4) adaptable in terms of NN properties, even classification dimensions.

The state of the art in NN design methodology can be split into two groups. The first group focuses on choosing the optimal NN *macrostructure* (e.g., Support Vector Machine versus Recurrent Neural Network). In the second group, there are guidelines and (semi)automated methods, that help find the optimal *microstructure* (e.g., number of hidden layers and neurons) of a selected macrostructure. The first group of approaches consists of guidelines and overview literature [5][6][7]. The problem (and virtue) with this set of methodologies is, that they require understanding of a vast set of NN concepts, before the designer is able to make an optimal choice. Dreyfus [5] states, for example: "No recipes will be provided here. It is our firm belief that no significant application can be developed without a basic understanding of the principles and methodology of model design and training." Of course, we agree with this position. However, it can be observed in practice, that there is a lack of systematic approach in choosing the macrostructure. As a consequence, Feedforward NN (FFNN) [1], learned with Backpropagation (BP) [21], is still chosen in the majority of applications, which we consider a negative trend [8]. The second group of approaches is necessary for the fine microstructural tuning of a chosen macrostructure (also usually demonstrated on FFNN with BP). These approaches are either given as a set of rules and recipes, or as an automated optimization tool. The most systematic approaches rely on the Design of Experiments (DoE) method, involving Taguchi principles [9][10][11]. Such methods systemize and automate the selection of, e.g., number of hidden layers or neurons, through experimenting with different setups. Similar methods are constructive and pruning algorithms, that add or remove neurons from an initial architecture [12][13]. Also, related are evolutionary strategies, which employ genetic operators for similar purposes [14][15][16].

Our proposed approach fits between these two groups and improves the results of both group's goals. It exhibits the main qualities of the second group (ability to automate the decision process) and applies them to the problematic of the first group (i.e., choosing the macrostructure), which is a crucial step in NN design, because the effect of any design actions depends greatly on early decisions. The aim of our proposed DSS is to improve the performance of NN-based based applications on

a large scale, through enabling designers to perform optimal early design decisions. Figure 2 illustrates how our proposed DSS improves the NN design process by enabling users to systematically find optimal NN instances for their application.

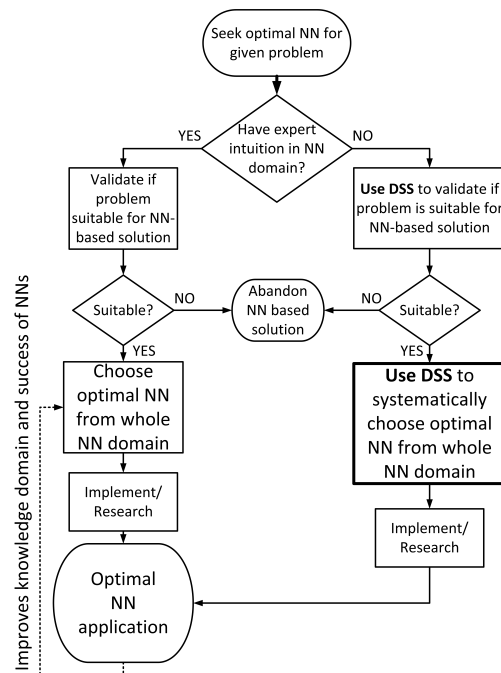


Figure 2. Our proposed DSS improves the NN design process by enabling users to systematically find optimal NN instances for their application.

At the heart of our proposed DSS is the taxonomic framework that facilitates a qualitative measure between NN instances. However, directly comparing NN instances from literature in detail is prohibitively problematic due to bias or lack of method in the description process [17]. In contrast to related taxonomic efforts, our taxonomy must thus provide a significant level of abstraction, allowing both a complete field overview and sufficient depth to aid qualitative comparison, while providing the flexibility for future adaptations of the proposed classification.

The Andrews-Diederich-Tickle (ADT) taxonomy [18] enables two NNs to be compared pairwise through *ADT*<sup>5</sup> criteria (defined by Andrews et al. [18] and refined by Tickle et al. [19]), but this taxonomy lacks orthogonality since some of its taxonomical categories (dimensions) are interdependent. Other taxonomies classify NNs purely through topology [20] or realization method [21]. And more recently, researchers create taxonomies that assist in choosing the best solution for the task [3][22] within a limited application area and solve locally what our work solves globally. Our generically specified ranking between feasible solutions permits us to deliver rule-of-thumb guidance that provides an excellent starting point for further in-depth analysis based on, e.g., *ADT*<sup>5</sup> criteria.

After review of DSS theory in existing literature, we decide to design our proposed DSS as a Knowledge-Driven DSS [23], as it fits our application best. Therefore, our Knowledge-Driven DSS will comprise the following components:

1. Knowledge base
2. User interface
3. Inference engine model
4. Communications component

Corresponding to the above components, our proposed system comprises the following: NN Knowledge base (Section III), 3D visualization of data and qualitative relations (Section IV-A), inference engine and qualitative relations in data (Section IV-B), interaction with 3D environment and entry of objective parameters (Section V), respectively.

## II. INFERENCE ENGINE DECISION SPACE

The main and fundamental result of our work is the conceptualization and theoretical foundation for the inference engine decision space (this Section) and knowledge base framework (Section III), that enables a global overview of the complete NN domain. The decision space, presented hereby, serves also as a coherent terminology and context for our knowledge base framework. Mathematical structure of interrelations must be well defined, to facilitate an effective inference engine, used in solving multiple-objective optimization problems [24]. The decision space is defined via the following descriptors of the NN knowledge domain:

- Set of NN instances  $\mathcal{I}$ : contains the subset of elements of the NN knowledge domain, which are neural networks. From the whole neural network knowledge domain (NNs, research initiatives, research groups, research goals, application areas, etc.), we gather concrete NN implementations and form the set of NN instances.
- NN classifier  $\zeta : \mathcal{I} \rightarrow \mathcal{P}$ : provides a classification of each member of  $\mathcal{I}$  into a particular set of groups  $\mathcal{P}$ .
- Property  $\mathcal{P}$ : the co-domain of a classifier  $\zeta$ , with the latter considered as a function.
- Property value  $p_i \in \mathcal{P}$ : a specific group of some classifier. It is given a name, which is then identified as this property value.
- NN framework  $\mathcal{F}$ : ordered list of classifiers relevant for a given user's interest.
- NN universe  $\mathcal{U}$ : defined by a framework  $\mathcal{F}$ , it is an  $|\mathcal{F}|$ -dimensional space, which is Cartesian product of the properties defined by the classifiers in  $\mathcal{F}$ .
- NN instance  $\mathcal{I}_i \in \mathcal{I}$ :  $\mathcal{I}_i = (p_1, \dots, p_f)$ ; an  $f$ -tuple of property values, each coming from its corresponding NN property.
- NN category  $\mathcal{C}_p \subseteq \mathcal{P}$ : subset of a specific property, containing a set of values (classifier groups) of this property. Possibly a singleton.
- NN landscape  $\mathcal{L} = \mathcal{C}_1 \times \mathcal{C}_2 \times \mathcal{C}_3 \times \dots \times \mathcal{C}_f$  with at least one  $\mathcal{C}_i$  being equal to the whole property  $\mathcal{P}_i$ . Subspace of a NN universe.
- NN type  $\mathcal{T} = \mathcal{C}_1 \times \mathcal{C}_2 \times \mathcal{C}_3 \times \dots \times \mathcal{C}_f$ : Cartesian product of categories. If all categories in the cartesian product are singletons, the NN type is also a NN instance.
- NN comparator  $\delta$ : innate comparative quality, defining a partial order  $>_\delta$  on the set of NN instances  $\mathcal{I}$ , by which some pairs of NN instances can be compared. In our

proposed DSS, NN comparators are chosen by defining the NN selection criteria (see section III). NN comparators are represented as colored arrows between NN types, with the color specifying different NN instance selection criteria and the thickness of the arrow proportional to number of evidence papers supporting the comparison.

- NN selection criteria  $\nabla$ : a set of possibly competing NN comparators used for comparison of NN instances.
- Pareto front  $\mathcal{R}$  of given NN selection criteria  $\nabla$ : a set of (discrete) NN instances  $j \in \mathcal{R}$  such that whenever some NN instance  $i \in \mathcal{I}$  is better than  $j$  with respect to some NN comparator  $\delta \in \nabla$ , i.e.,  $j >_\delta i$ , then there is some other comparator  $\delta' \in \nabla$ , such that  $i >_{\delta'} j$ , i.e.,  $i$  is better than  $j$  w.r.t.  $\delta'$ . In other words, a NN instance belongs to the Pareto front of  $\nabla$ , if it cannot be improved over without harming at least one of the NN selection criteria in  $\nabla$ .

What signifies our approach is the decision to abandon the aim for back-to-back comparison of specific NN implementations via rigid criteria (which would limit us to NN research subdomains) and employ a flexible DSS, enabling self-organization of data and allowing the evolution of the framework, together with the evolution of knowledge base contents.

## III. TAXONOMY FOR KNOWLEDGE BASE

With the inference engine decision space theoretically defined in Section II, we proceed to determine the principal dimensions for classification of NN instances. As no single source provides a definitive field overview, we as first step systematically create a taxonomic blueprint for our knowledge base. We define the NN classifiers  $\zeta$  as operators for sorting of NN instances into main taxonomic branches:

- $\zeta_1$  Implementation Platform
- $\zeta_2$  NN Architecture
- $\zeta_3$  Learning Paradigm
- $\zeta_4$  Learning Algorithm
- $\zeta_5$  Learning Task

Using our defined NN classifiers, we proceed to build the taxonomy. For its core, we extract the classification used in the book Neural Networks: A Comprehensive Foundation [4], which offers a wide overview of main concepts in NN domain. To build upon this core, we add the overviews of evolutionary methods [25], Spiking Neural Networks [26] and a recent 20-years overview of hardware-friendly neural networks [27]. A principal quality of our system lies in our choice of high abstraction when defining the taxonomy; e.g., while there exist numerous flavors of the BP algorithm, our taxonomy does not differentiate between them. Only by obscuring a such detail, we can achieve a domain-wide overview. Still, as the field of NNs is very diverse, an ultimate taxonomy requires broader community collaboration and finally, consensus; both of which exceed the scope of this work.

We find that our chosen NN classifiers map NN instances into NN properties (i.e., sets of NN categories  $\mathcal{C}$ , possibly singletons)  $\mathcal{P}_1, \mathcal{P}_2, \mathcal{P}_3, \mathcal{P}_4$  and  $\mathcal{P}_5$ , respectively:

$\mathcal{P}_1$  ( $\zeta_1$ : **Implementation Platform**) takes values from:

- General Purpose ( $\mathcal{C}_1^1$ ): Software Simulation on general purpose computer of Von Neumann Architecture (CPU), Digital Signal Processor (DSP) Graphical Processing Unit (GPU), Supercomputer (SCP)
- Dedicated Hardware ( $\mathcal{C}_2^1$ ): Field Programmable Gate Array (FPGA), Neural Hardware / Neural Processing Unit (NPU), Analog Implementation (ANLG), Application Specific Integrated Circuit (ASIC)

$\mathcal{P}_2$  ( $\zeta_2$ : **NN Architecture**) takes values from:

- Feedforward Neural Network (FFNN)
- Second Generation NNs ( $\mathcal{C}_2^2$ ): Recurrent Neural Network (RNN), Long Short-Term Memory (LSTM)
- Spiking Neural Network (SNN)
- Cellular Neural Network (CNN)
- Self-organizing Map (SOM)
- Reservoir Networks (RSVN) ( $\mathcal{C}_6^2$ ): Echo-state Network (ESN), Liquid-state Machine (LSM)
- Convolutional NN (CONN)
- Deep Belief Network (DBN)
- Hybrid (HYB)

$\mathcal{P}_3$  ( $\zeta_3$ : **Learning Paradigm**) takes values from:

- Supervised Learning (SUP)
- Reinforcement Learning (REINF)
- Unsupervised Learning (UNSUP)
- Genetic Learning (GENL)

$\mathcal{P}_4$  ( $\zeta_4$ : **Learning Algorithm**) takes values from:

- Error Correction ( $\mathcal{C}_1^4$ , ECR): Backpropagation (BP), Extended Kalman Filter (EKF), Stochastic Gradient Descent (SGD),
- Hebbian Learning (HBL)
- Competitive Learning (CPL)
- Evolutionary ( $\mathcal{C}_4^4$ , EVOL): Evolution of Architecture (EVLARCH), Evolution of Weights (EVLWT), Evolution of Learning Algorithm (EVLALG)
- Reservoir Computing (RSV)
- Hybrid (HYB)

$\mathcal{P}_5$  ( $\zeta_5$ : **Learning Task**) takes values from:

- Pattern Association ( $\mathcal{C}_1^5$ ): Autoassociation (PASCAUT), Heteroassociation (PASCHET)
- Pattern Recognition ( $\mathcal{C}_2^5$ , PREC): Natural Language Processing (NLP), Principal Component Analysis (PCA), Speech (SPC), Dimensionality Reduction (DRED), Spatio-temporal (SPT)
- Control ( $\mathcal{C}_3^5$ , CTL): Indirect (CTLIND), Direct (CTLDIR)
- Function Approximation ( $\mathcal{C}_5^5$ , FAPPROX): System Identification (SYSID), Inverse System (INVSYS)
- Classification (CSF)
- Regression (RGR)

Property  $\mathcal{P}_2$  thus comprises 11 NN property values, gathered in 9 categories, of which  $\mathcal{C}_2^2$  and  $\mathcal{C}_6^2$  each contain two property values;  $\mathcal{C}_2^2$  contains  $p_2$  and  $p_3$  and  $\mathcal{C}_6^2$  contains  $p_7$  and  $p_8$ . Property value indices run free from category indices.

The presented property values and categories can be further manipulated and refined. However, to enable efficient domain

overview, a significant level of abstraction is required. For further detailed inspection, more specialized taxonomies can be used (see Section I). For example, the Backpropagation learning algorithm has a multitude of variants [17], but for a comprehensive overview, abstraction is crucial.

A. *Qualitative comparison through NN selection criteria*  $\nabla$

With the taxonomic backbone defined, we can proceed with classification of NN instances from processed literature through property values  $\mathcal{P}$ , using our set of NN classifiers  $\zeta$ . This comparative dimension, well-defined but very permitting, is a core facility of our knowledge base and the heart of our DSS' inference engine. Therefore, we also extract from literature sources the qualitative comparison information between NN instances w.r.t. the following set of chosen NN selection criteria  $\nabla$ :

$\delta_1$  **Low cost of ownership** (feasibility, practicality, low hardware cost, low development complexity, presence of user community)

$\delta_2$  **Capability** (effectiveness, convergence speed, generalization performance, benchmark success, high learning rate, low error)

$\delta_3$  **Real-time requirement** (speed of execution, on-line vs. off-line learning, pre-learned vs. adaptive learning)

$\delta_4$  **Design maturity** (proven solution vs. emerging technology)

While estimates for all NN criteria can be extracted from literature or provided by a domain expert, design maturity could also be automatically calculated as a measure of occurrence frequency in literature.

B. *5-letter notation and knowledge base formation*

In the 5-dimensional NN universe, defined by our NN framework  $\mathcal{F}$ , that we define in Section III through selecting our set of NN classifiers  $\zeta_{1,\dots,5}$ , each NN instance is described via five NN properties  $\mathcal{P}_{1,\dots,5}$ . Therefore, each element in the database compares two NN instances or NN landscapes in terms of five parameters. To construct our formal notation, we build upon the idea of 3-letter notation used in the theory of scheduling problems [28] and adapt it to a 5-letter notation for describing NN instances. Our resulting formal representation of relation(s) between two NN instances is as follows:

$$(\mathcal{P}_1, \mathcal{P}_2, \mathcal{P}_3, \mathcal{P}_4, \mathcal{P}_5) >_{\delta_{i,\dots,n}} (\mathcal{P}'_1, \mathcal{P}'_2, \mathcal{P}'_3, \mathcal{P}'_4, \mathcal{P}'_5), \quad (1)$$

where each NN property  $\mathcal{P}_{1,\dots,5}$  can be a comma-separated list of elements (NN property values),  $n$  is the total number of selection criteria and where  $i, i \in \{1 \dots n\}$  denotes the group of indices of NN qualifiers, by which the 'greater' NN instance is superior to the 'lesser' NN instance.

In our knowledge database, the following example statement extracted from a scientific source [27]: "FPGA is a superior implementation platform to ASIC in terms of flexibility and cost for implementations of FFNN or RNN with supervised or reinforcement learning, using stochastic learning algorithms." is formally denoted as follows:

$$(\mathcal{P}_1[4], \mathcal{P}_2[3, 4], \mathcal{P}_3[1, 2], \mathcal{P}_4[3], \mathcal{P}_5[x]) >_{\delta_2} (\mathcal{P}_1[6], \mathcal{P}_2[3, 4], \mathcal{P}_3[1, 2], \mathcal{P}_4[3], \mathcal{P}_5[x]), \quad (2)$$

Or:

$$\begin{aligned}
 & (FPGA, \{FFNN, RNN\}, \{SUP, REINF\}, \\
 & \quad SGD, x) \\
 & >_{\delta_{cost, flexibility}} \\
 & (ASIC, \{FFNN, RNN\}, \{SUP, REINF\}, \\
 & \quad SGD, x)
 \end{aligned} \quad (3)$$

This example also illustrates the case where the paper does not specify all property values (in this example, the learning task  $\mathcal{P}_5[x]$ ), the statement is incomplete and it may mean either that the relation is indifferent to that property, or that there is no information present about that property's role in the relationship. After reviewing selected literature (e.g., [27][29][25][30]–[36]), we get a number of such specific statements that comprise our knowledge base seed information, which serves as basis for development of our inference engine and visualization scheme.

#### IV. RESULT: KNOWLEDGE-DRIVEN DSS WITH INFERENCE ENGINE AND VISUALIZATION TOOL

The proposed inference engine, together with knowledge base visualization, are the final results of our efforts presented in this paper. Both modules operate on the data in the knowledge database in a read-only fashion. In the following subsections, we present our scheme for exploratory visualization of our multidimensional knowledge database and describe our interactive inference engine.

##### A. Visualization scheme

Every point in the NN universe's graphical representation corresponds to one NN instance. The most valuable information in our knowledge database is the qualitative comparison between NN instances. This is shown in Figure 3, illustrating the graphical representation of Statement (3) from Section III-B. We have found, that using three dimensions for the visualization is optimal, because it allows users to navigate the environment interactively and to recognize interdependencies, even after switching between the chosen set of three dimensions. The 3D visualization can only represent three dimensions at a time and the user can explore the NN knowledge domain using any dimension set.

Figure 4 shows the 3D representation our NN universe  $\mathcal{U}$ , containing points from our prototype knowledge base. This view allows users to examine the NN knowledge domain in a full 3D environment, visually exploring (through zoom and rotation of view around any axis) the comparative relations between NN instances. Axes correspond to NN properties  $\mathcal{P}$ ; each dot corresponds to a single NN instance  $\mathcal{I}_i$ ; arrows represent qualitative comparators  $\delta_{1...4}$  between two NN instances; arrow thickness and dot size indicate the quantity of source papers (database entries) for the shown information; call-out-type labels are references to source literature. Each of the selection criteria is assigned its own arrow color (red, magenta, blue and black for  $\delta_1$ ,  $\delta_2$ ,  $\delta_3$  and  $\delta_4$ , respectively). Coloring of NN instances aids in visual comparison (blue is

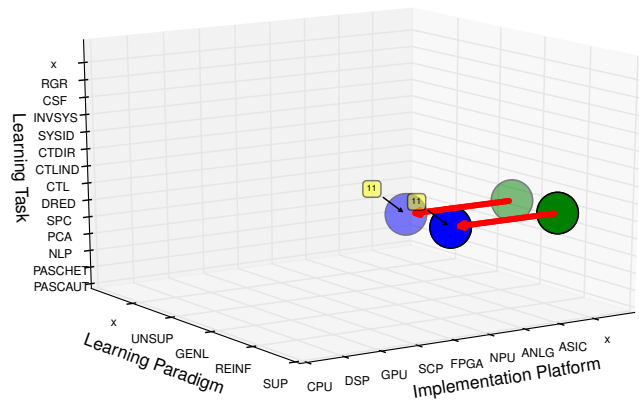


Figure 3. Example graphical representation of qualitative relation between two NN instances. The figure represents Statement (3) from Section III-B.

better, green is worse). Using the inference engine (Section IV-B), the visualization can be actively augmented according to the user's decision input.

##### B. Inference Engine

Our inference engine approaches our NN instance selection process as a multiple-objective optimization problem [24] and applies a Pareto front method [37], using our Pareto front  $\mathcal{R}$ , as defined in Section II, to find the suitable, multiple, non-dominant solutions. After the user specifies their boundary conditions and sets weights of the NN selection criteria  $\nabla$  through the graphical user interface, the DSS automatically identifies the discrete-equivalent of Pareto front  $\mathcal{R}$  and the user can directly locate and examine the source literature, relating the NN instances in  $\mathcal{R}$ . Rating of alternatives is based on a weighted pairwise comparison matrix [38], resulting in levels within a discrete-space equivalent of Pareto front, which guide the user towards NN instances, specified as superior with respect to their criteria. The user can iteratively and interactively further fine-tune the selection of best candidates via weights of their criteria  $\nabla$ , to determine the optimal NN instance for their problem, until the final choice is made. Information, inferred by the inference engine, is also used as input into the visualization tool, to augment the database visualization by superimposing relationships, marking Pareto points and their scores, hiding a subset of NN instances, etc. (see Figure 5). Both the visualization tool and the inference engine can be extended with additional inference and visualization functions. Section V gives further insight into the typical application of the inference engine, through step-by-step explanation.

#### V. PRACTICAL EXAMPLE OF DSS USE

The two major user groups that can gain remarkable benefits from using our proposed DSS, are **Industry Practitioner** and **Academic Researcher**. Both user groups share the main interest of finding the optimal NN instance for their scenario, but have a different angle: a) the industry practitioner's goal is to find the **best fitting, well proven** NN implementation

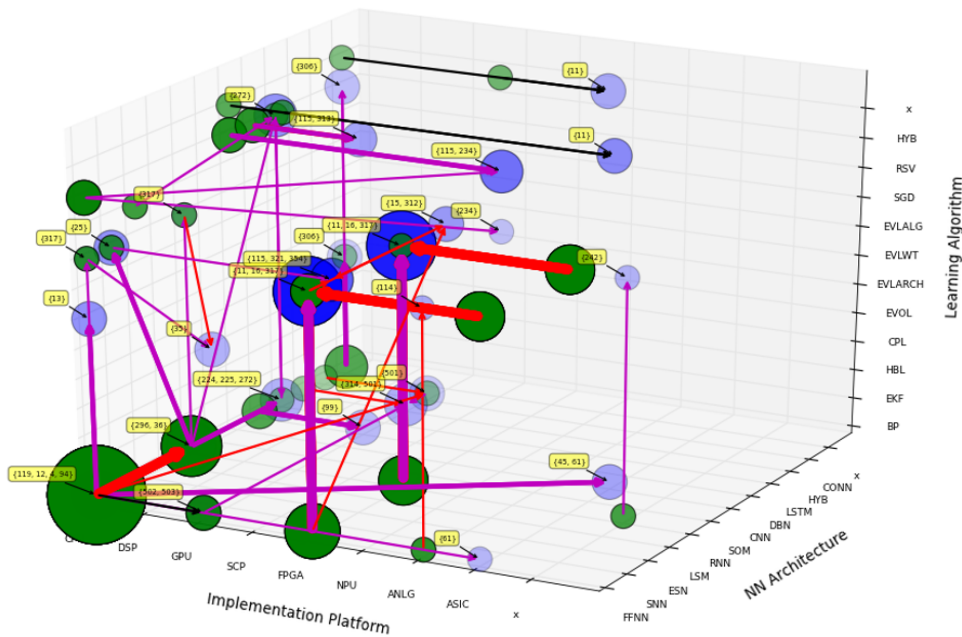


Figure 4. The 3D representation our NN universe  $\mathcal{U}$ , containing points from our prototype knowledge base. See Section III for axis label definitions.

for their **application** (with set boundary conditions on task type, implementation platform, etc.), and b) the academic researcher’s aim is to find an active research area or synergies between domains, to systematically selects the most meaningful **research direction**. In this section, we illustrate step-by-step a typical use case for the industry practitioner. Let our example demand a **highly accurate** and **real-time capable** NN instance for image-based **object recognition** using **supervised learning**. The following steps illustrate how this ground truth is used with our DSS as decision input and how the inference engine results are interpreted and used:

1) *Enter task requirements into DSS*: the practitioner enters their set of boundary conditions by selecting the NN instance properties, that are defined by the application. In our example, these are the learning task and learning paradigm. The DSS considers these two properties as pivots, therefore, only the **remaining** three properties (dimensions) are shown in the 3D visualization tool (Figure 5a). After the axes are determined, the user specifies pivot axis values (learning task = classification, CSF and learning paradigm = supervised, SUP). The effect of this is shown in Figure 5b, where only those NN instances are shown, whose pivot property values are as specified by the user. Thus, this step narrows down the search down to three dimensions and defines the NN landscape, which optimal solutions can be chosen from. If more than two pivot axes are specified by the use case, the NN landscape is 2- or 1-dimensional, further focusing the search.

2) *Set weights for selection criteria  $\nabla$* : once the 3D NN landscape is defined in the previous step, the user specifies weights for each of  $\nabla$  within the range from -5 to 5. In our example, the selected weights for  $\delta_{1..4}$  are 2, 5, 5 and 3, respectively (see Section III-A for list of criteria).

3) *Examine Pareto front  $\mathcal{R}$* : based on weighted criteria, the inference engine extracts NN instances, that belong to the

discrete Pareto front  $\mathcal{R}$ . These are NN instances, for which there is no NN instance superior w.r.t. any of the selection criteria (no arrows leaving the NN instance). These points are highlighted by the DSS via black squares. For better viewing of the points in  $\mathcal{R}$ , the user can interact with the 3D view by rotation around any axis. This is seen in 5c (left), showing the  $\mathcal{R}$  points in an updated view, obtained by rotating 5b around the 'view rotation axis' in the indicated direction. In the lower left corner of each  $\mathcal{R}$ -marking is the NN instance’s score (closeup view in Figure 5c, right), calculated by the inference engine using the weighted pairwise comparison matrix.

4) *Analyze top alternative in Pareto front*: the user chooses the highest-ranking NN instances in the Pareto frontier and analyzes their corresponding source literature, indicated by call-outs (see Figure 3). Our example gives the highest score of 12 to NN instance, described in database entries 314 and 502 (Figure 5c). From corresponding source papers [32] and [33], the practitioner learns, that a) FFNNs can be used as convolution NNs, b) GPU implementation in [33] has better flexibility than previously known implementations, c) GPU implementation of CONN has better real-time capabilities than CPU implementation, d) Hybrid between pure CONN and FFNN has better recognition performance than any of these two used alone, e) hybrid implementation in [33] has won an impressive series of image classification competitions, etc.

In conclusion, based on the industry practitioner’s input criteria, the DSS recommends, that a GPU-based hybrid CONV-FFNN NN should be investigated as best choice for the given use case. This simple case illustrates how a user can, using our DSS in a few simple steps, rapidly traverse an immensely diverse knowledge base, in order to choose an optimal direction for further investigation, and finally, concrete implementation.



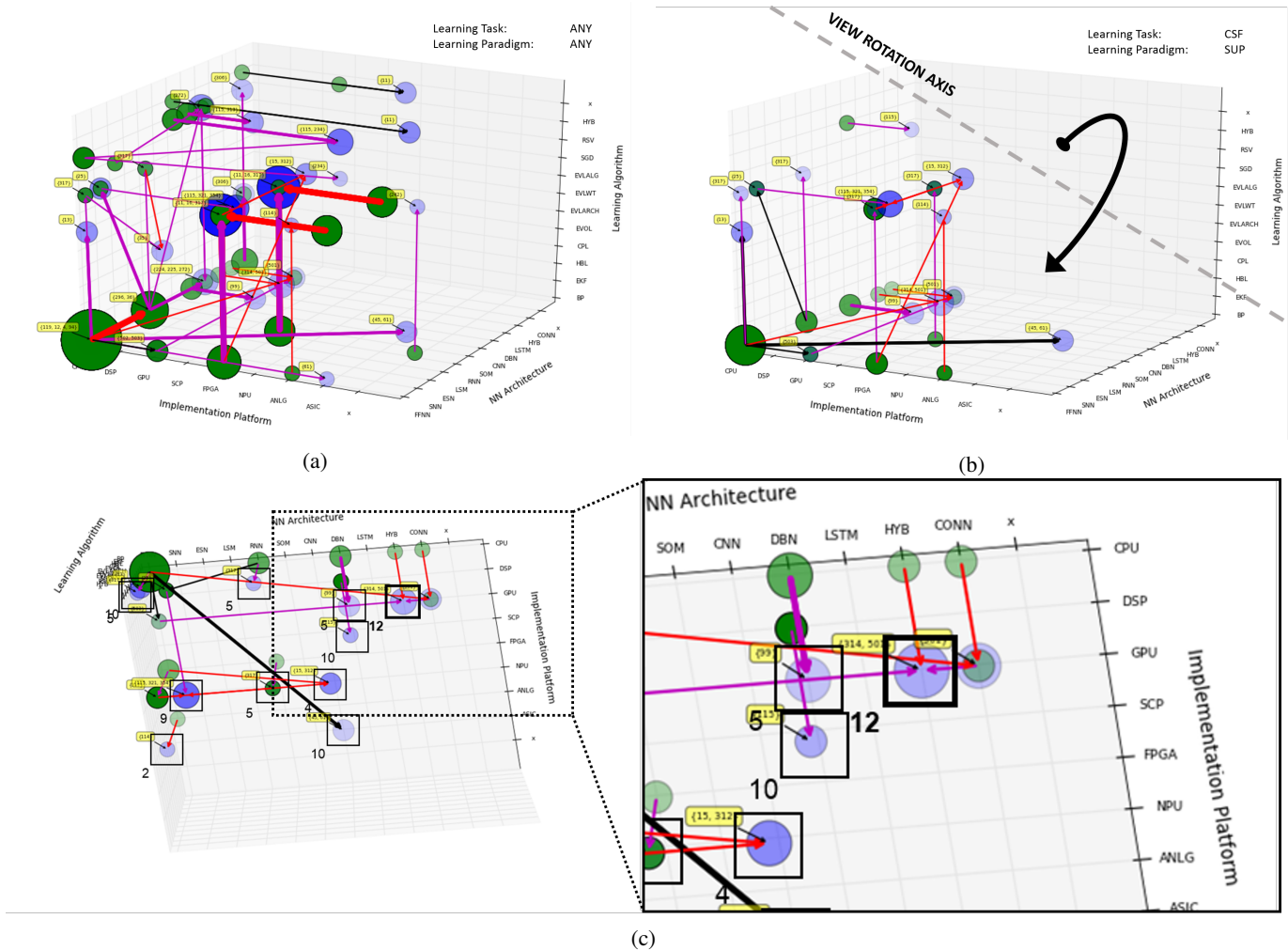


Figure 5. Rapid assessment of complete knowledge domain. Typical step-by-step application of the inference engine, together with the visualization scheme, used for finding an optimal NN instance, based on user input parameters.

VI. CONCLUSION AND FUTURE WORK

In this work, we have identified the need for an abstract-level overview of the NN knowledge domain and alleviate the barriers, which an industry practitioner or researcher meet, when selecting the right NN instance or research direction for their specific scenario. We devised a theoretical foundation for a decision support system, comprising a knowledge database and inference engine, that can automate the decision process of choosing the best NN architecture for the task at hand. We also presented a prototype implementation and a proof-of-concept through step-by-step use of our DSS. This illustrated its potential in aiding users to exploit the whole knowledge of NN research domain and improve NN results in research and industry, through choosing optimal approaches to machine learning problems.

In our future work, we will study how the inference engine could be expanded to automatically find promising combinations of NN properties, based on current highest-scoring NN instances within the database. This will enable our system to automatically highlight synergies between existing approaches.

Future work also includes making the knowledge base and its visualized interaction accessible online. Moderated, collaborative editing of the knowledge base among researchers is also considered. Once the knowledge base reaches critical mass, researchers will be motivated to contribute their own work, or populate it with entries where they notice a lack of coverage. An editorial group could, on a per need basis, revise the taxonomy when novel NN properties or categories emerge. The proposed 5-letter notation enables automatic parsing of the literature, keeping the knowledge database up-to-date at all times and solving this problem once and for all. An automatically-generated dynamic survey paper could always be kept up-to-date and available in printed form for a quick overview of recent developments.

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## REFERENCES

- [1] K. Hornik, M. Stinchcombe, and H. White, "Multilayer feedforward networks are universal approximators," *Neural networks*, vol. 2, no. 5, 1989, pp. 359–366.
- [2] B. M. Wilamowski, "Neural network architectures and learning algorithms," *Industrial Electronics Magazine, IEEE*, vol. 3, no. 4, 2009, pp. 56–63.
- [3] H. Jacobsson, "Rule extraction from recurrent neural networks: A taxonomy and review," *Neural Computation*, vol. 17, no. 6, 2005, pp. 1223–1263.
- [4] B. Taylor and J. Smith, "Validation of neural networks via taxonomic evaluation," in *Methods and Procedures for the Verification and Validation of Artificial Neural Networks*. Springer US, 2006, pp. 51–95.
- [5] G. Dreyfus, "Modeling with neural networks: Principles and model design methodology," in *Neural Networks*. Springer Berlin Heidelberg, 2005, pp. 85–201.
- [6] A. Omondi and J. C. Rajapakse, *FPGA Implementations of Neural Networks*. Springer Netherlands, 2006.
- [7] Y. Huang, "Advances in artificial neural networks—methodological development and application," *Algorithms*, vol. 2, no. 3, 2009, pp. 973–1007.
- [8] C. Moraga, "Design of neural networks," in *Knowledge-Based Intelligent Information and Engineering Systems*. Springer, 2007, pp. 26–33.
- [9] J. Ortiz-Rodríguez, M. Martínez-Blanco, and H. Vega-Carrillo, "Robust design of artificial neural networks applying the taguchi methodology and doe," in *Electronics, Robotics and Automotive Mechanics Conference*, 2006, vol. 2. IEEE, 2006, pp. 131–136.
- [10] E. Inohira and H. Yokoi, "An optimal design method for artificial neural networks by using the design of experiments," *JACIII*, vol. 11, no. 6, 2007, pp. 593–599.
- [11] J. F. Khaw, B. Lim, and L. E. Lim, "Optimal design of neural networks using the taguchi method," *Neurocomputing*, vol. 7, no. 3, 1995, pp. 225 – 245.
- [12] J.-f. Qiao, Y. Zhang, and H.-g. Han, "Fast unit pruning algorithm for feedforward neural network design," *Applied Mathematics and Computation*, vol. 205, no. 2, 2008, pp. 622–627.
- [13] H. Han and J. Qiao, "A self-organizing fuzzy neural network based on a growing-and-pruning algorithm," *Fuzzy Systems, IEEE Transactions on*, vol. 18, no. 6, 2010, pp. 1129–1143.
- [14] S. G. Mendivil, O. Castillo, and P. Melin, "Optimization of artificial neural network architectures for time series prediction using parallel genetic algorithms," in *Soft Computing for Hybrid Intelligent Systems*. Springer, 2008, pp. 387–399.
- [15] Z.-j. Zheng and S.-q. Zheng, "Study on a mutation operator in evolving neural networks," *Journal of Software*, vol. 13, no. 4, 2002, pp. 726–731.
- [16] G. G. Yen, "Multi-objective evolutionary algorithm for radial basis function neural network design," in *Multi-Objective Machine Learning*. Springer, 2006, pp. 221–239.
- [17] M.-T. Vakil-Baghmisheh and N. Pavesic, "A fast simplified fuzzy artmap network," *Neural Processing Letters*, vol. 17, no. 3, 2003/06/01 2003, pp. 273–316.
- [18] R. Andrews, J. Diederich, and A. B. Tickle, "Survey and critique of techniques for extracting rules from trained artificial neural networks," *Knowledge-Based Systems*, vol. 8, no. 6, 1995, pp. 373–389.
- [19] A. Tickle, R. Andrews, M. Golea, and J. Diederich, "The truth will come to light: directions and challenges in extracting the knowledge embedded within trained artificial neural networks," *Neural Networks, IEEE Transactions on*, vol. 9, no. 6, 1998, pp. 1057–1068.
- [20] E. Fiesler, "Neural network classification and formalization," *Computer Standards & Interfaces*, vol. 16, no. 3, 1994, pp. 231–239.
- [21] R. Rojas, "Neural networks: A systematic introduction," Springer, 1996.
- [22] H. R. Maier, A. Jain, G. C. Dandy, and K. P. Sudheer, "Methods used for the development of neural networks for the prediction of water resource variables in river systems: Current status and future directions," *Environmental Modelling & Software*, vol. 25, no. 8, 2010, pp. 891–909.
- [23] D. J. Power, *Decision support systems: concepts and resources for managers*. Greenwood Publishing Group, 2002.
- [24] N. Xiong and M. L. Ortiz, "Principles and state-of-the-art of engineering optimization techniques," in *ADVCOMP 2013, The Seventh International Conference on Advanced Engineering Computing and Applications in Sciences*, 2013, pp. 36–42.
- [25] S. Ding, H. Li, C. Su, J. Yu, and F. Jin, "Evolutionary artificial neural networks: a review," *Artificial Intelligence Review*, 2013, pp. 1–10.
- [26] S. Ghosh-Dastidar and H. Adeli, "Spiking neural networks," *International Journal of Neural Systems*, vol. 19, no. 04, 2009, pp. 295–308.
- [27] J. Misra and I. Saha, "Artificial neural networks in hardware: A survey of two decades of progress," *Neurocomputing*, vol. 74, no. 1-3, 2010, pp. 239–255.
- [28] R. L. Graham, E. L. Lawler, J. K. Lenstra, and A. Rinnooy Kan, "Optimization and approximation in deterministic sequencing and scheduling: a survey," *Annals of Discrete Mathematics*. v5, 1977, pp. 287–326.
- [29] L. Fortuna, P. Arena, D. Balya, and A. Zarandy, "Cellular neural networks: a paradigm for nonlinear spatio-temporal processing," *Circuits and Systems Magazine, IEEE*, vol. 1, no. 4, 2001, pp. 6–21.
- [30] J. Schmidhuber, D. Wierstra, M. Gagliolo, and F. Gomez, "Training recurrent networks by evoluno," *Neural Computation*, vol. 19, no. 3, 2007, pp. 757–779.
- [31] G. Andrienko et al., "Space-in-time and time-in-space self-organizing maps for exploring spatiotemporal patterns," *Computer Graphics Forum*, vol. 29, no. 3, 2010, pp. 913–922.
- [32] J. Stallkamp, M. Schlipsing, J. Salmen, and C. Igel, "the german traffic sign recognition benchmark: a multi-class classification competition," in *Neural Networks (IJCNN), The 2011 International Joint Conference on*. IEEE, 2011, pp. 1453–1460.
- [33] D. Cireşan, U. Meier, J. Masci, and J. Schmidhuber, "Multi-column deep neural network for traffic sign classification," *Neural Networks*, vol. 32, no. 0, 2012, pp. 333–338.
- [34] R. Raina, A. Madhavan, and A. Y. Ng, "Large-scale deep unsupervised learning using graphics processors," in *ICML*, vol. 9, 2009, pp. 873–880.
- [35] D. Coyle, "Neural network based auto association and time-series prediction for biosignal processing in brain-computer interfaces," *Computational Intelligence Magazine, IEEE*, vol. 4, no. 4, 2009, pp. 47–59.
- [36] R. K. Al Seyab and Y. Cao, "Nonlinear system identification for predictive control using continuous time recurrent neural networks and automatic differentiation," *Journal of Process Control*, vol. 18, no. 6, 2008, pp. 568–581.
- [37] M. Farshbaf and M.-R. Feizi-Derakhshi, "Multi-objective optimization of graph partitioning using genetic algorithms," in *Advanced Engineering Computing and Applications in Sciences*, 2009. ADVCOMP '09. Third International Conference on, Oct 2009, pp. 1–6.
- [38] S. Ghodspour and C. O'Brien, "A decision support system for supplier selection using an integrated analytic hierarchy process and linear programming," *International Journal of Production Economics*, vol. 56–57, no. 0, 1998, pp. 199 – 212, production Economics: The Link Between Technology And Management.